

# Numerical studies of cloud turbulence – from mesoscale moist convection to cloud microphysics

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# Outline

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- Motivation
- Characteristic scales of cloud dynamics
- Direct numerical simulation studies
  - Mesoscale: cloud patterns in moist Boussinesq convection
  - Microscale: turbulent entrainment and droplet microphysics
- Outlook

Joint work with:

[Paul Götzfried](#) (TU Ilmenau)

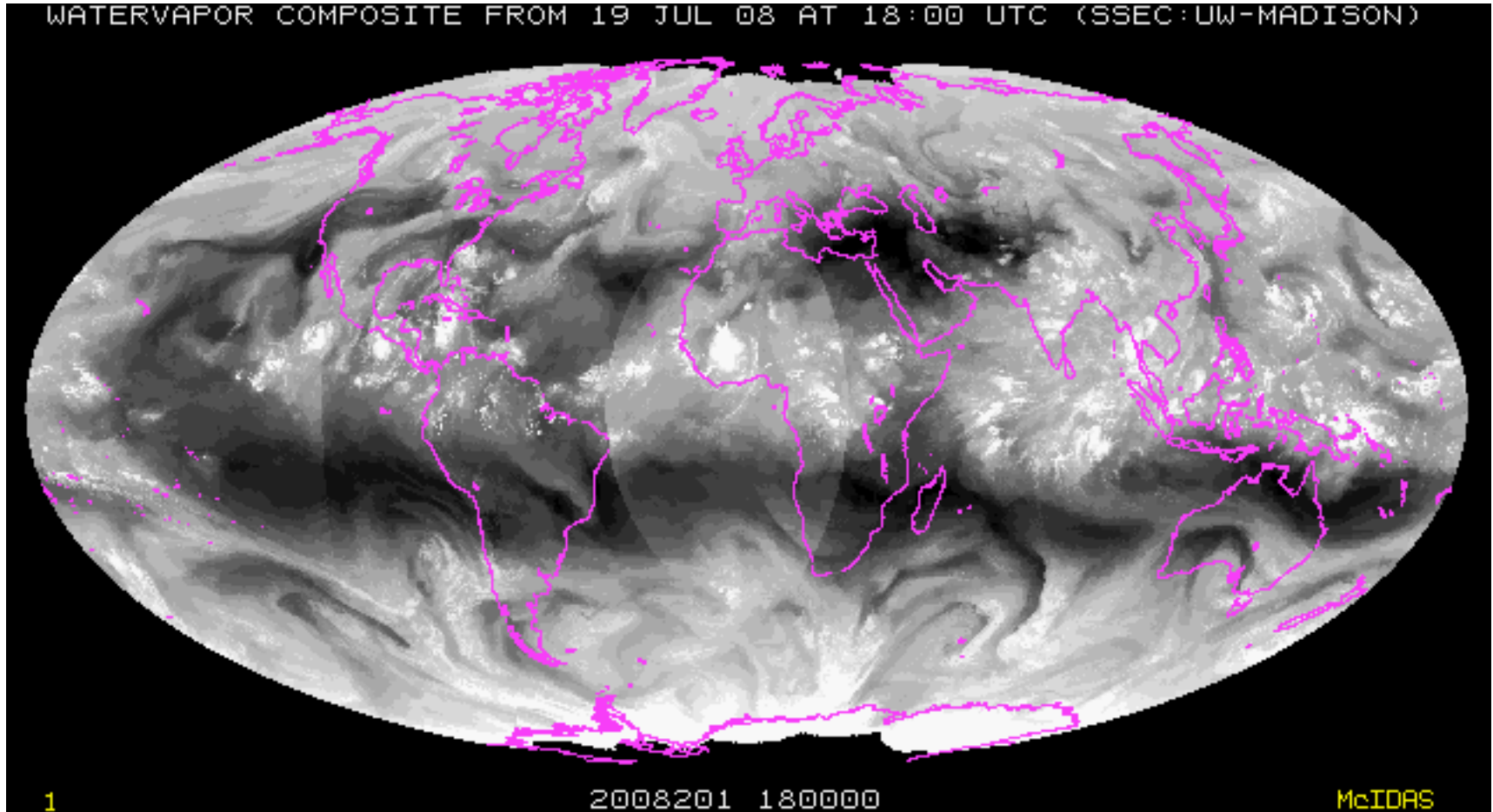
[Bipin Kumar](#) (Indian Institute of Tropical Meteorology Pune)

[Olivier Pauluis](#) (New York University)

[Raymond A. Shaw](#) (Michigan Technological University Houghton)

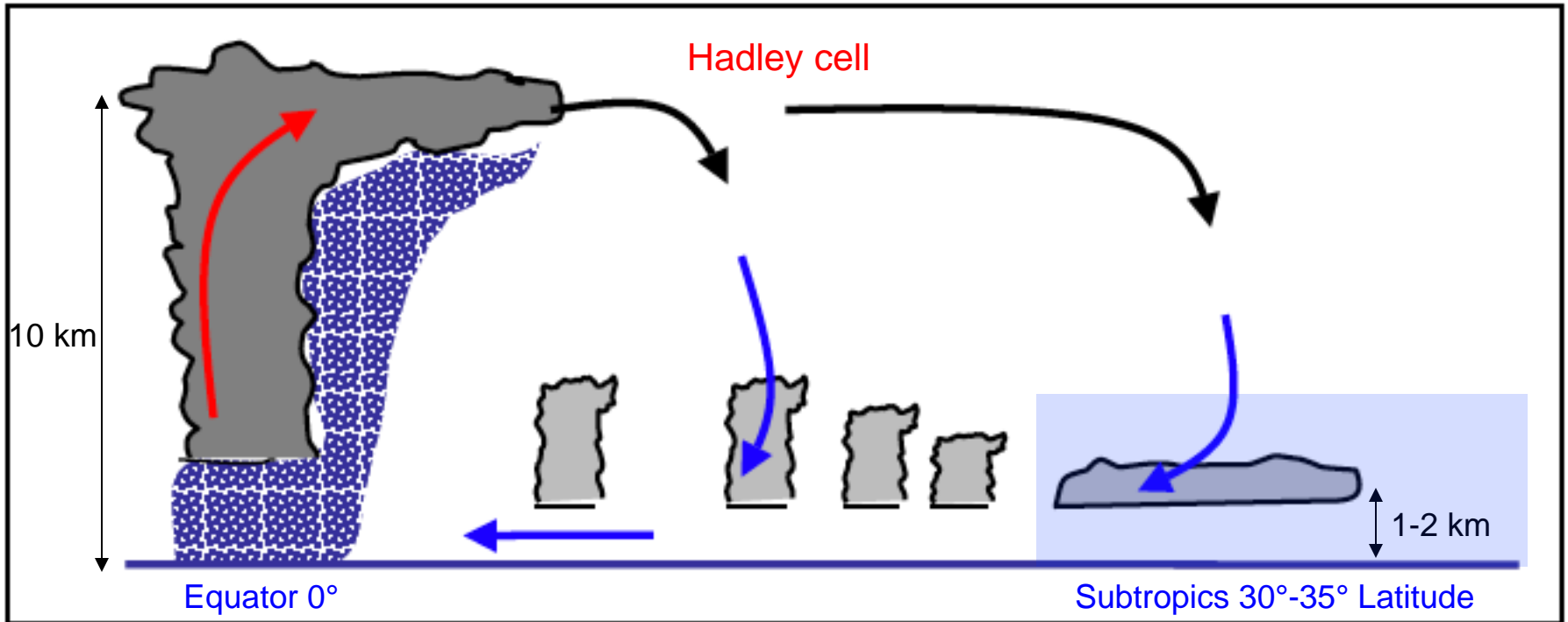
[Thomas Weidauer](#) (Friedrich Schiller University Jena)

# Atmospheric convection



Formation of clouds in the atmosphere

# Deep and shallow convection

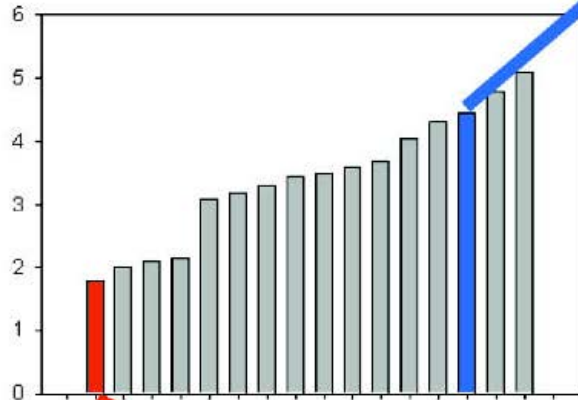


# Low cloud parametrization in climate models

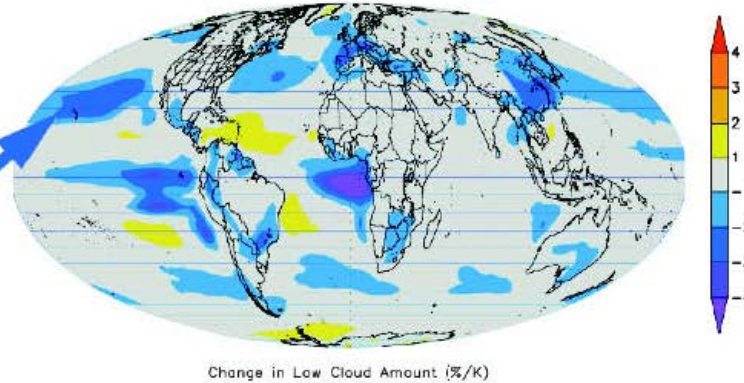
Stephens, *J. Climate* 2005

Which feedback results from a fixed 1% per year increase of CO<sub>2</sub> concentration?

Predicted warming from 16 GCMs in K

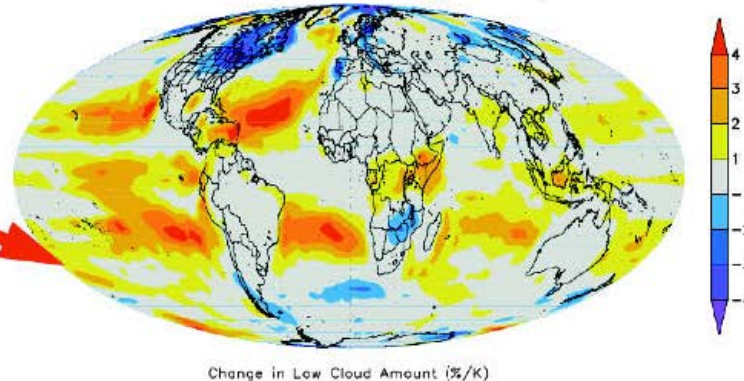


GFDL AM2-ML (2xCO<sub>2</sub> - CTRL)



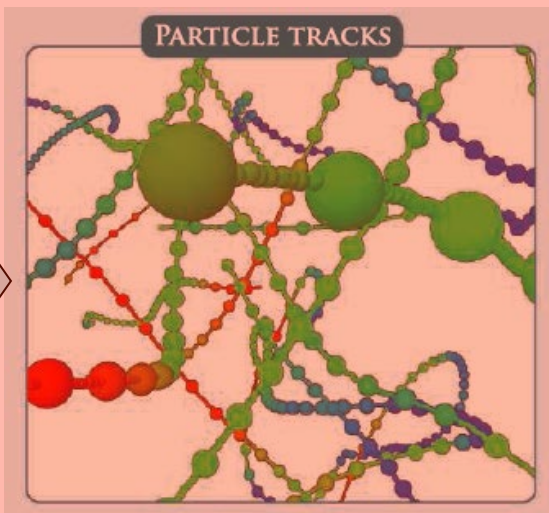
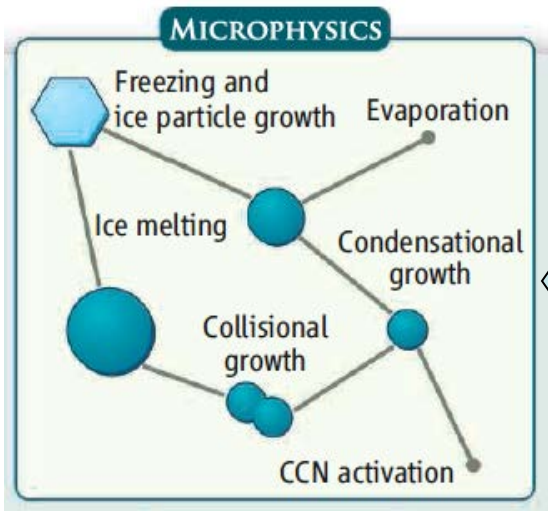
20 year average of change of low cloud amount (in % per K)

NCAR CAM2 (Year70 @1%CO<sub>2</sub>/yr - CTRL)

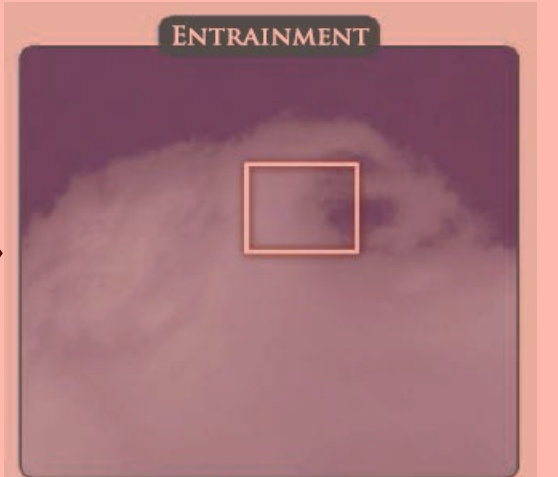
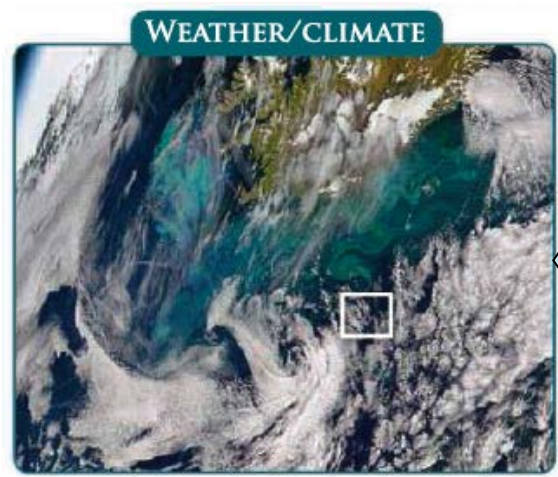


GCM=Global Circulation Model

# Turbulence in clouds



1mm to 1km



# Typical scales in a cloud

- Cloud droplet radius  $r = 10^{-5} m$
  - Largest scale of turbulence  $L \sim 10^3 m$
  - Smallest scale of turbulence  $\eta_K \sim 10^{-3} m$
  - Characteristic velocity  $U \sim 1 m/s$
- $$\left. \begin{array}{l} L \sim 10^3 m \\ \eta_K \sim 10^{-3} m \\ U \sim 1 m/s \end{array} \right\} Re = \frac{UL}{\nu} \sim 10^8 \Rightarrow Re_\lambda \sim 10^4$$
- Lifetime of cloud  $T_L \sim 10^3 s$
  - Shortest time scale  $\tau_\eta \sim 50 ms$
  - Particle inertia effects  $St = \frac{\tau_p}{\tau_\eta} = \frac{2\rho_l r^2}{9\rho_v \eta_K^2} \sim 2 \times 10^{-2}$
  - Gravitational settling  $Sv = \frac{\tau_p g}{v_\eta} = \frac{2\rho_l r^2 g \tau_\eta}{9\rho_v \nu \eta_K} \sim 10^{-1}$
  - Droplet Evaporation  $Da_\eta = \frac{\tau_\eta}{\tau_{phase}} \sim 10^{-2}$
  - $Da_L = \frac{T_L}{\tau_{phase}} \sim 100$

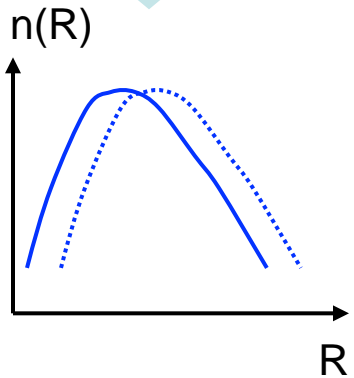
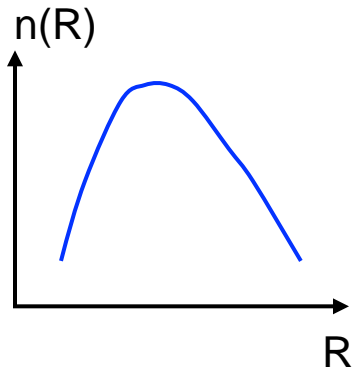
Turbulent mixing in clouds = multiscale + multiphysics

# Homogeneous vs. inhomogeneous mixing

Burnet & Brenguier, *J. Atmos. Sci.* 2007; Lehmann, Siebert & Shaw, *J. Atmos. Sci.* 2009

Homogeneous mixing

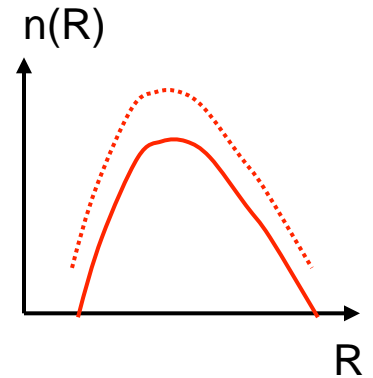
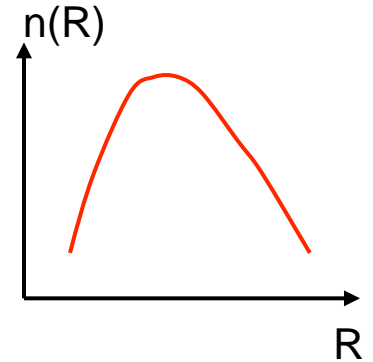
$$Da \ll 1$$



All droplets shrink slowly in well-mixed environment

Inhomogeneous mixing

$$Da \gg 1$$



Droplets at the edge evaporate completely while those inside cloud remain unchanged

$$Da = \frac{\tau_{fluid}}{\tau_{phase}}$$

Damköhler number

Turbulence = Continuum of  $\tau_{fluid}$

Both regimes are relevant !





## **Part 1**

# **Moist Rayleigh-Bénard convection simulations at cloud mesoscale**

# Boussinesq equations for moist convection

*Bannon, J. Atmos. Sci. 2001*

Mass balance	$\nabla \cdot \vec{u} = 0$
Momentum balance	$\partial_t \vec{u} + (\vec{u} \cdot \nabla) \vec{u} = -\frac{1}{\rho_0} \nabla p + \nu \nabla^2 \vec{u} + \vec{f}$
Energy balance	$\partial_t T + (\vec{u} \cdot \nabla) T = \kappa \nabla^2 T + \frac{L}{c_p} C_d$
Vapor mixing ratio	$\partial_t q_v + (\vec{u} \cdot \nabla) q_v = \kappa_v \nabla^2 q_v - C_d$
Liquid water mixing ratio	$\partial_t q_l + (\vec{u} \cdot \nabla) q_l = C_d$
	$\vec{f} = g \left[ \frac{T - T_0}{T_0} + \left( \frac{R_v}{R_d} - 1 \right) (q_v - q_{v0}) - q_l \right] \vec{e}_z$

plus b.c. & model to determine condensation rate  $C_d$

Additional space- and time-dependent latent heat release or evaporative cooling

# Boussinesq equations for shallow clouds

*Bannon, J. Atmos. Sci. 2001*

No fallout of rain

Ice-free clouds

Compressibility effects are negligible due to low heights

$$\begin{aligned} \text{Mass balance} & \quad \nabla \cdot \vec{u} = 0 \\ \text{Momentum balance} & \quad \partial_t \vec{u} + (\vec{u} \cdot \nabla) \vec{u} = -\frac{1}{\rho_0} \nabla p + \nu \nabla^2 \vec{u} + \vec{f} \\ \text{Energy balance} & \quad \partial_t T + (\vec{u} \cdot \nabla) T = \kappa \nabla^2 T + \frac{L}{c_p} C_d + Q_{rad} \\ \text{Total water mixing ratio} & \quad \partial_t q_T + (\vec{u} \cdot \nabla) q_T \simeq \kappa_v \nabla^2 q_T \end{aligned}$$

$$\vec{f} = \vec{f}(T, q_T, z)$$

plus b.c. & model to determine condensation rate  $C_d$

# Simple thermodynamics of phase changes

Bretherton, *J. Atmos. Sci.* 1987, 1988; Pauluis & JS, *Comm. Math. Sci.* 2010

What is the least set of moist convection equations to describe cloud formation processes?

■ Nearly adiabatic motion  $T \rightarrow S$

■ Total water content

$$q_T = q_l + q_v$$

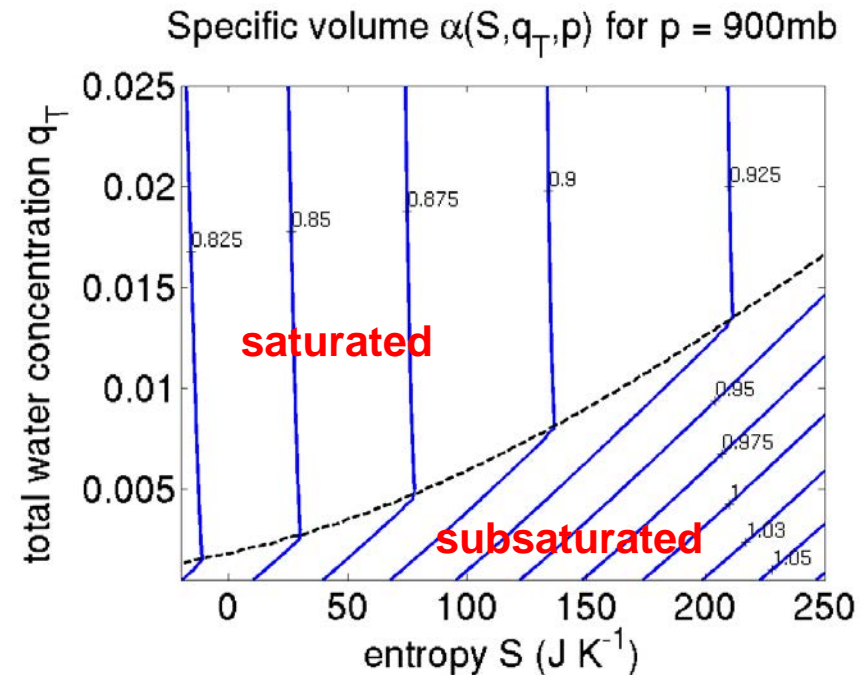
■ Piecewise linear equation of state

$$(S, q_T, p) \rightarrow (D, M)$$

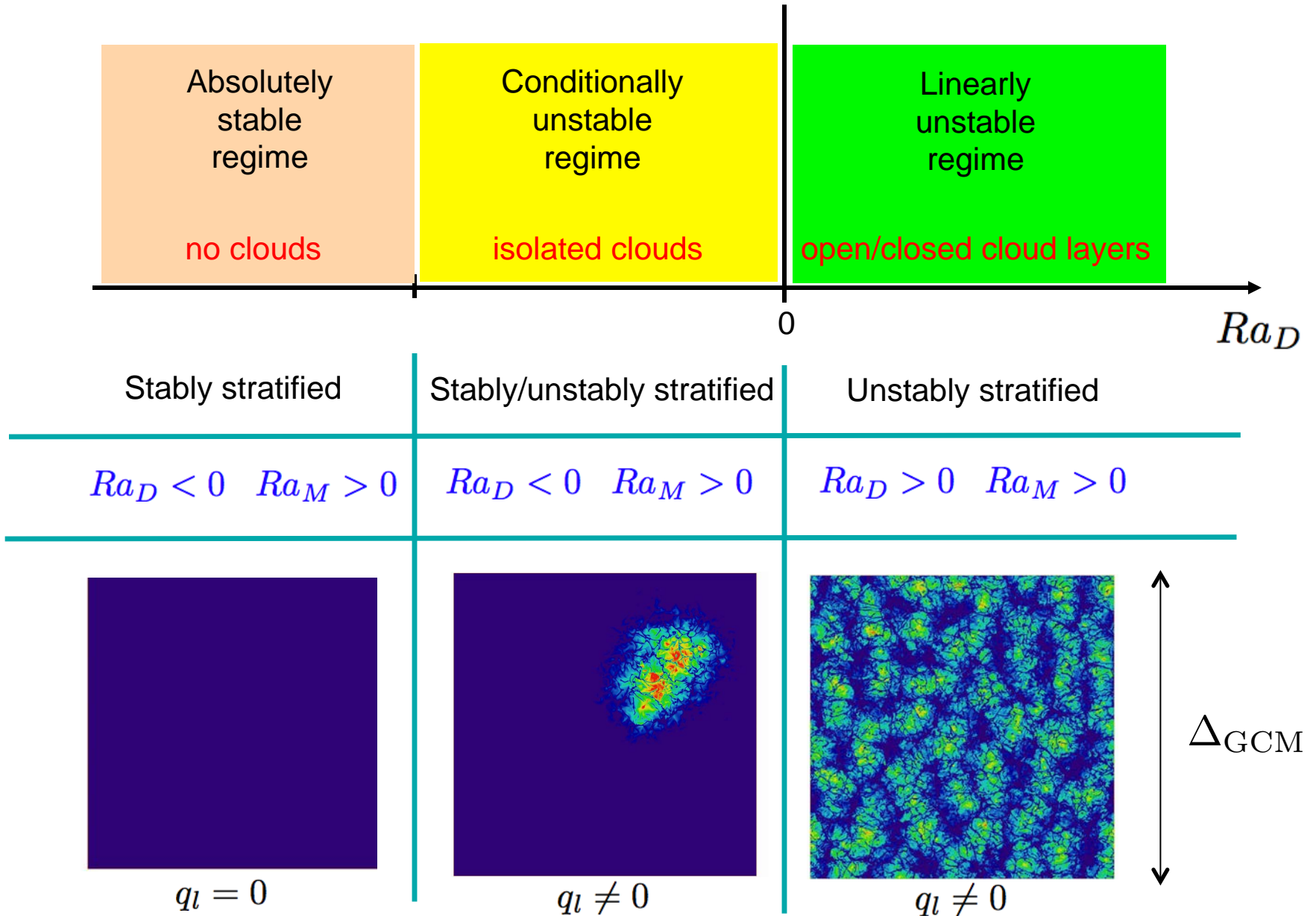
■ Simple saturation condition without supersaturation

■ DNS in a large-aspect ratio layer

Two buoyancy fields  $D$  and  $M$  with  $Ra_D$  and  $Ra_M$



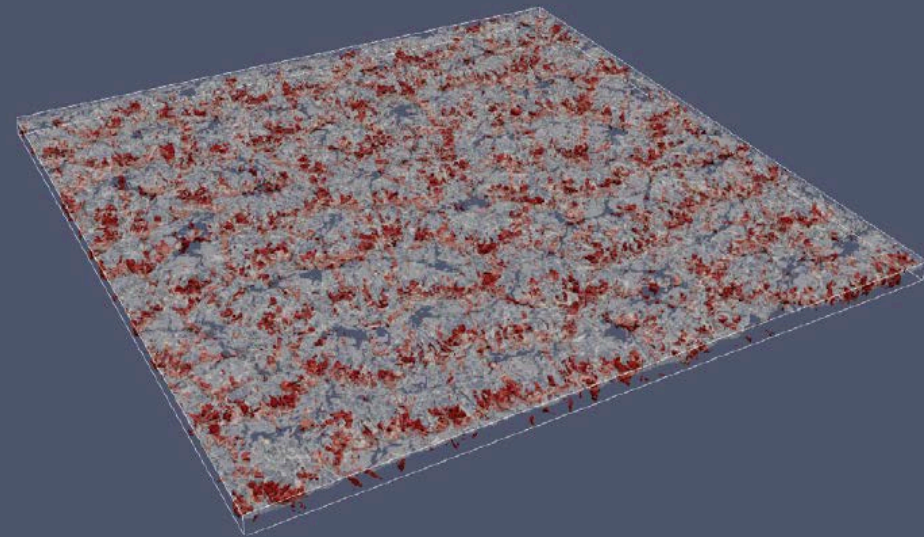
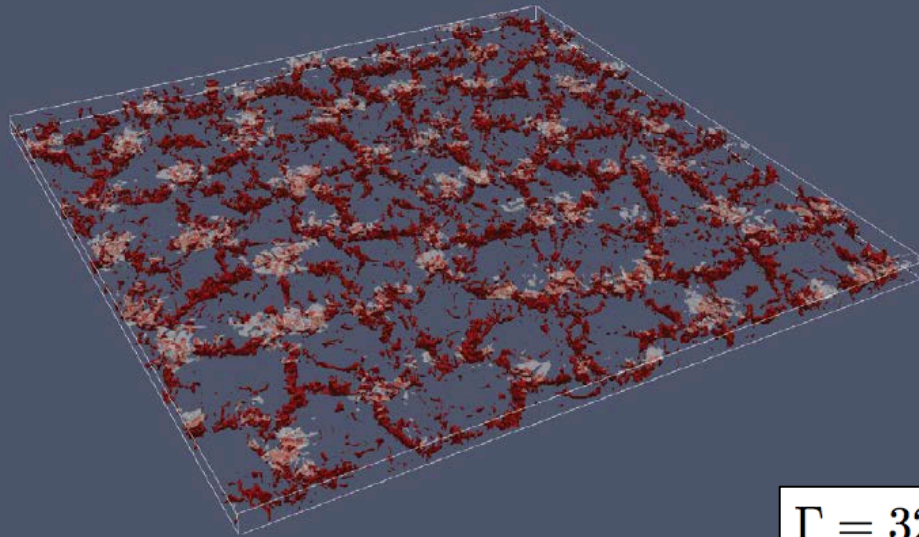
# Three regimes of moist RB convection



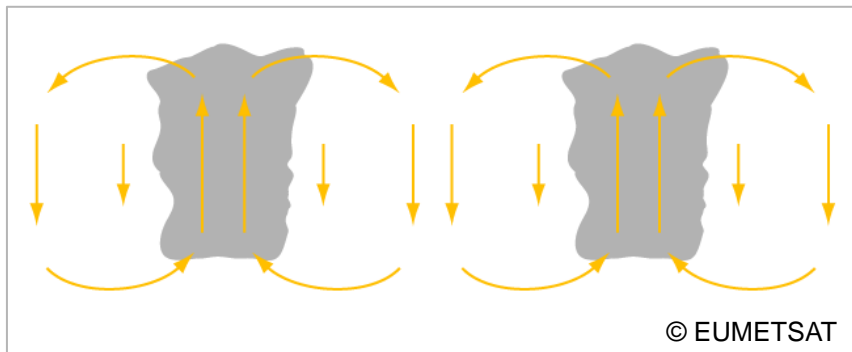
# Linearly unstable regime

*Weidauer, Pauluis & JS, New J. Phys. 2010*

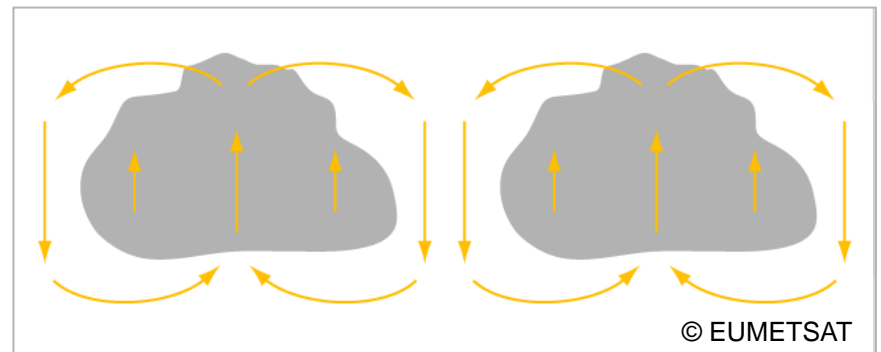
Cloud cover determined by the cloud water deficit at the top boundary



$$\Gamma = 32$$



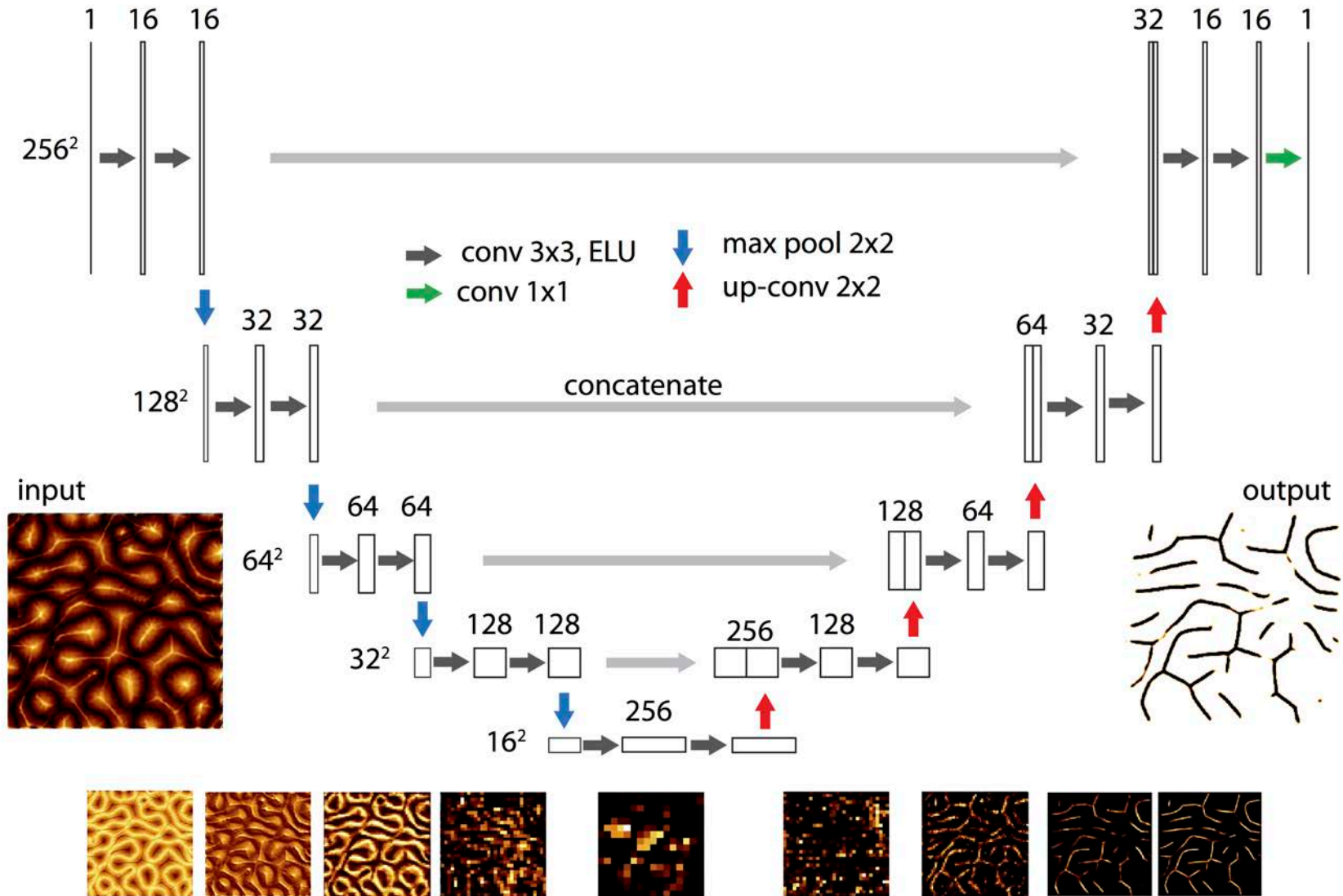
Open Cell Convection



Closed Cell Convection

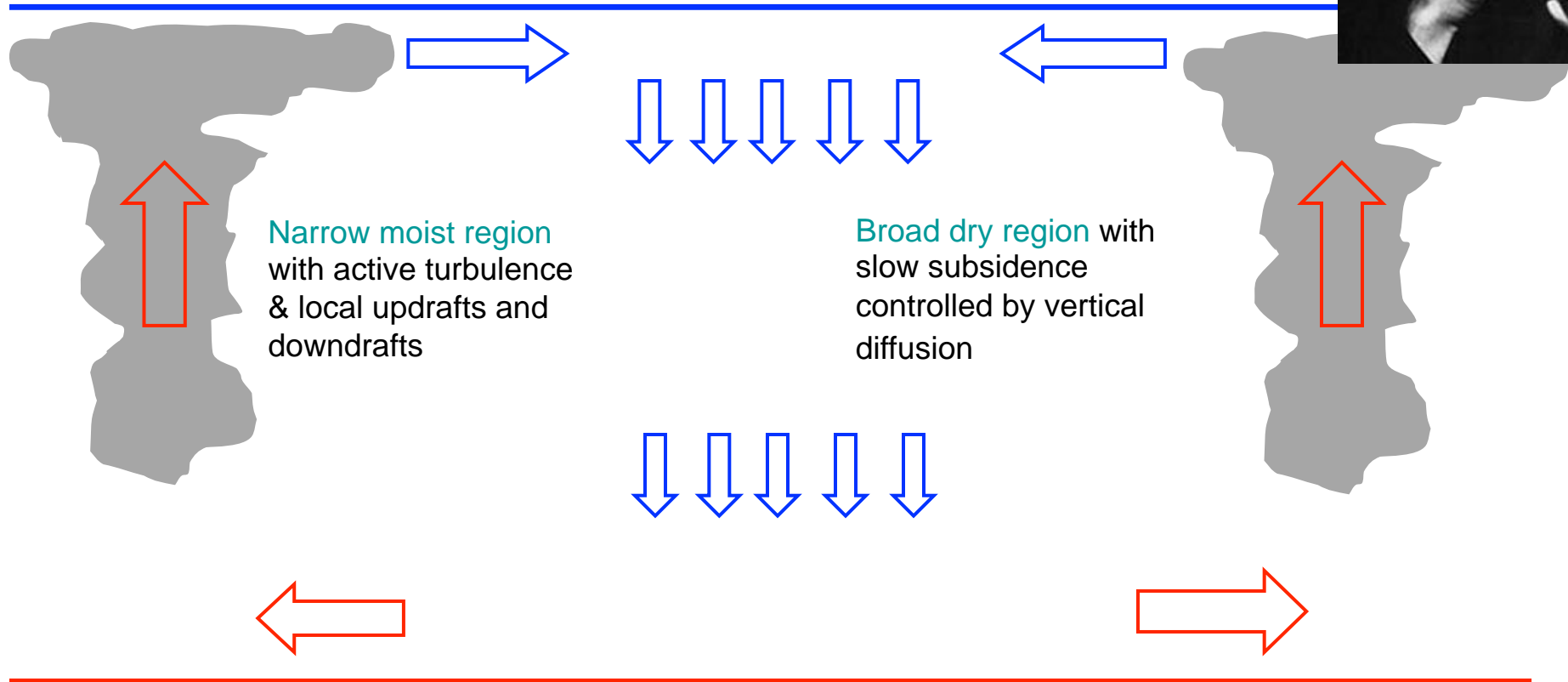
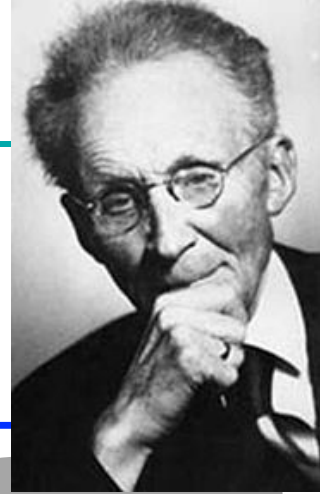
# Turbulent transport networks in dry convection

Pandey, Scheel & JS, Nat. Commun. 2018



# Conditionally unstable regime

Bjerknes, *Quat. J. Royal Meteor. Soc.* 1938

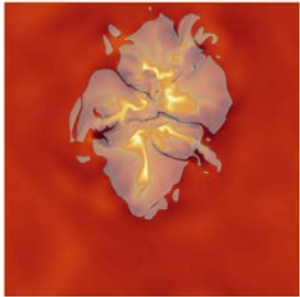


$$6 \text{ K km}^{-1} \sim \Gamma_m < \Gamma = \left| \frac{d\bar{T}}{dz} \right| < \Gamma_d = 10 \text{ K km}^{-1}$$

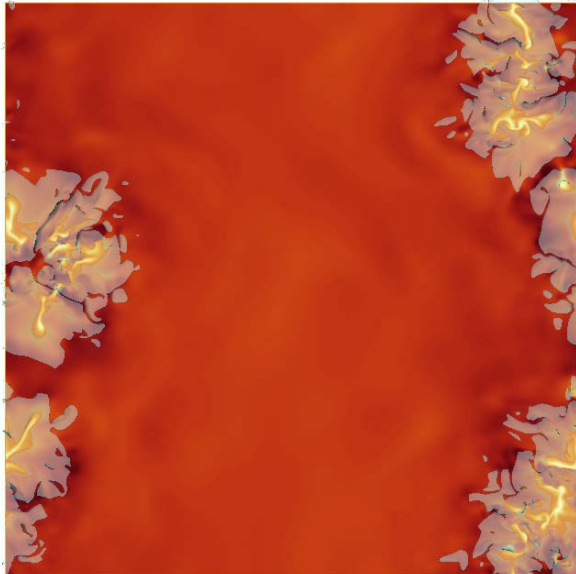


# Cloud aggregation

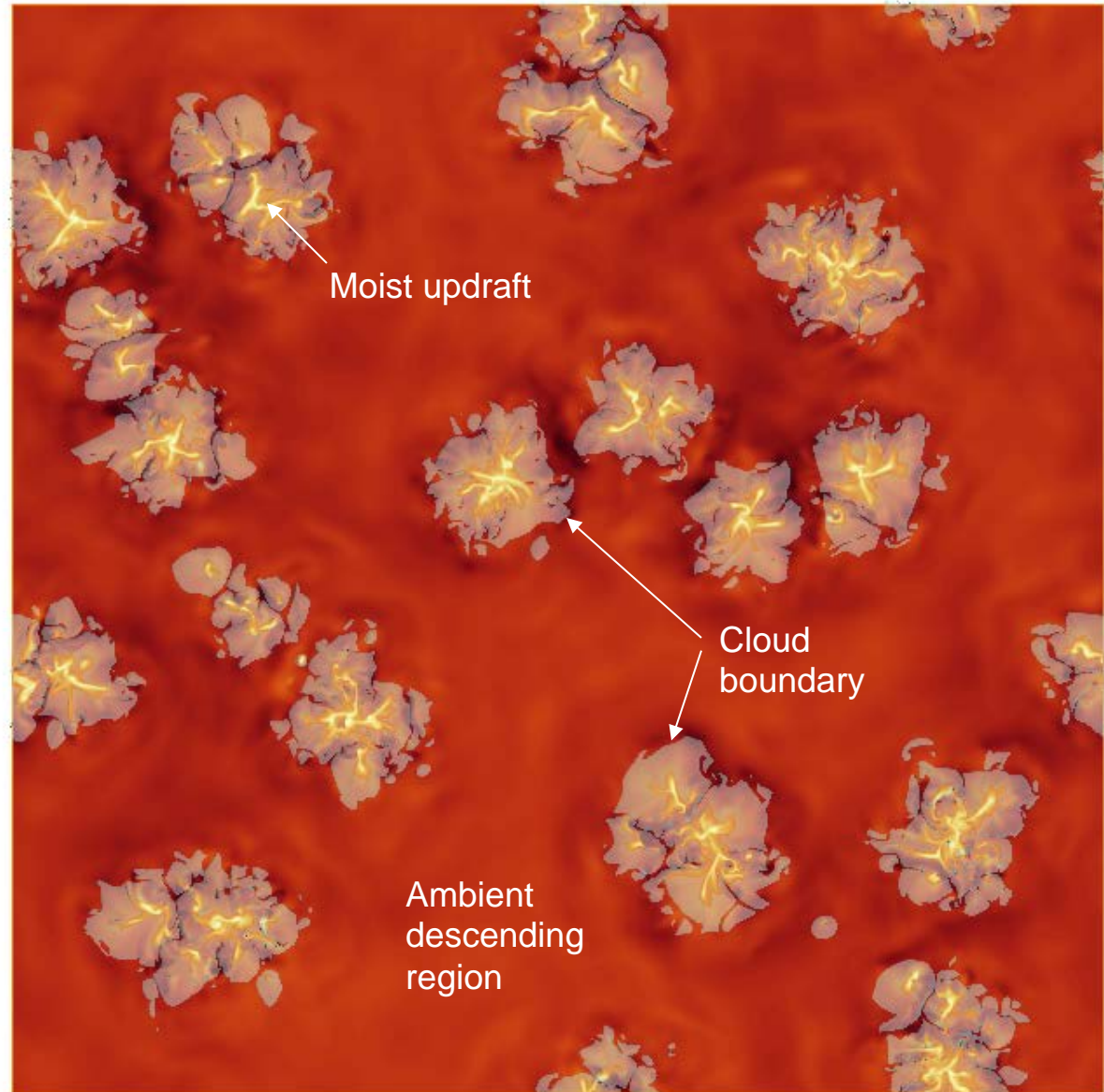
*Pauluis & JS, PNAS 2011*



$\Gamma = 16$



$\Gamma = 32$



$\Gamma = 64$

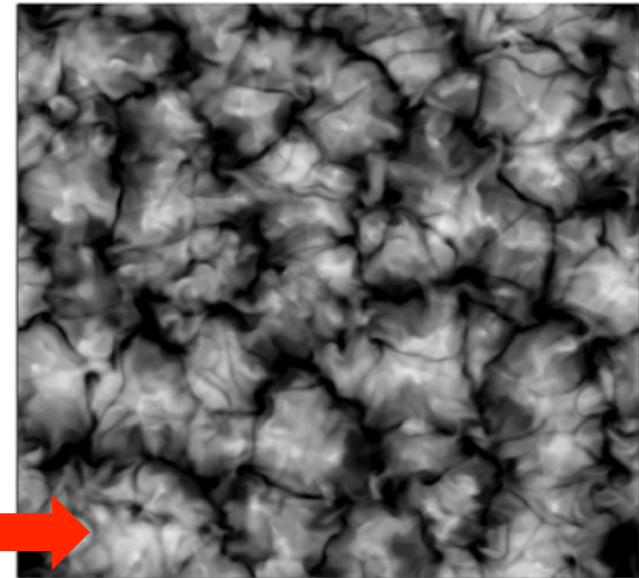
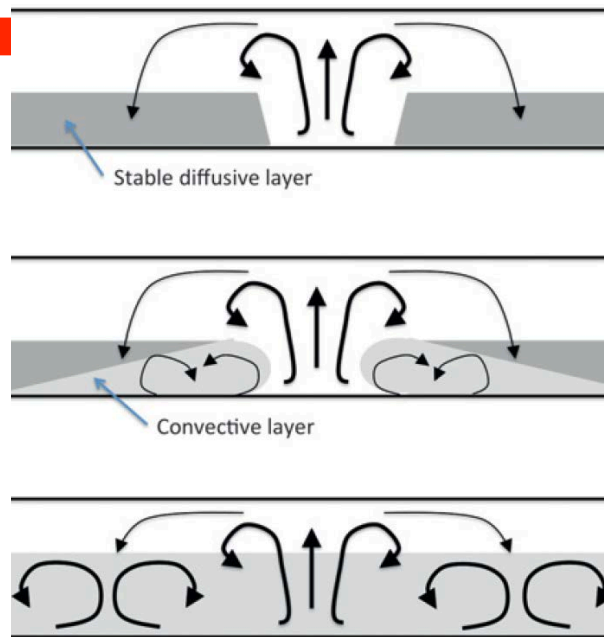
# Additional radiative cooling

Pauluis & JS, *J. Atmos. Sci.* 2013

$$\text{LWP} = \int_0^H q_l dz$$



No cooling



Strong cooling

Additional radiative cooling destabilizes lower diffusion layer and enhances heat transfer and cloud formation



- Simplest extension of Rayleigh-Bénard convection to moist convection with phase changes
- Study of cloud turbulence in cumulus or stratocumulus-type regimes
- Analysis of pattern formation and related variability of moist buoyancy fluxes at mesoscale

O. Pauluis and JS, *Comm. Math. Sci.* 8, 295 (2010).

JS and O. Pauluis, *J. Fluid Mech.* 648, 509 (2010).

T. Weidauer, O. Pauluis, and JS, *New J. Phys.* 12, 105002 (2010).

O. Pauluis and JS, *PNAS* 108, 12623 (2011).

T. Weidauer, O. Pauluis, and JS, *Phys. Rev. E* 84, 046303 (2011).

T. Weidauer and JS, *Phys. Fluids* 24, 076604 (2012).

O. Pauluis and JS, *J. Atmos. Sci.* 70, 1187 (2013).

T. Weidauer and JS, *New J. Phys.* 15, 125025 (2013).



## **Part 2**

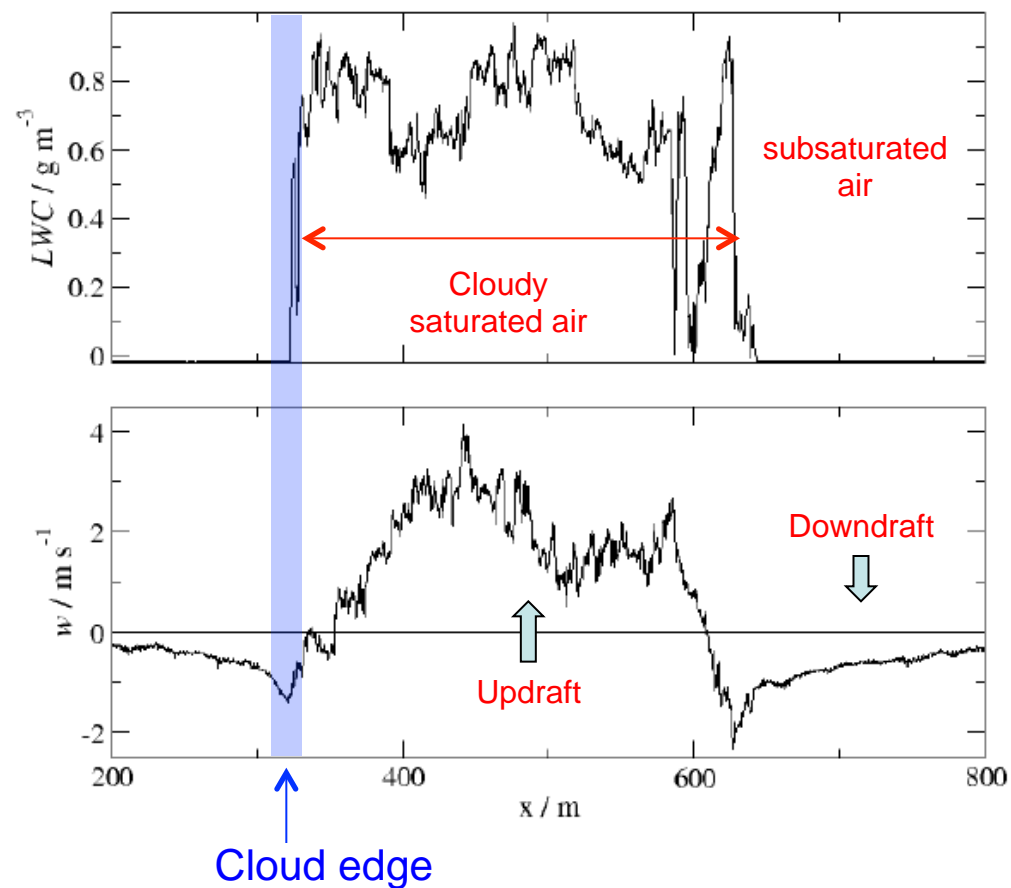
# **Euler-Lagrangian simulations at cloud microscale**

# Helicopter-based field measurements

Siebert et al., Atmos. Chem. Phys. 2013

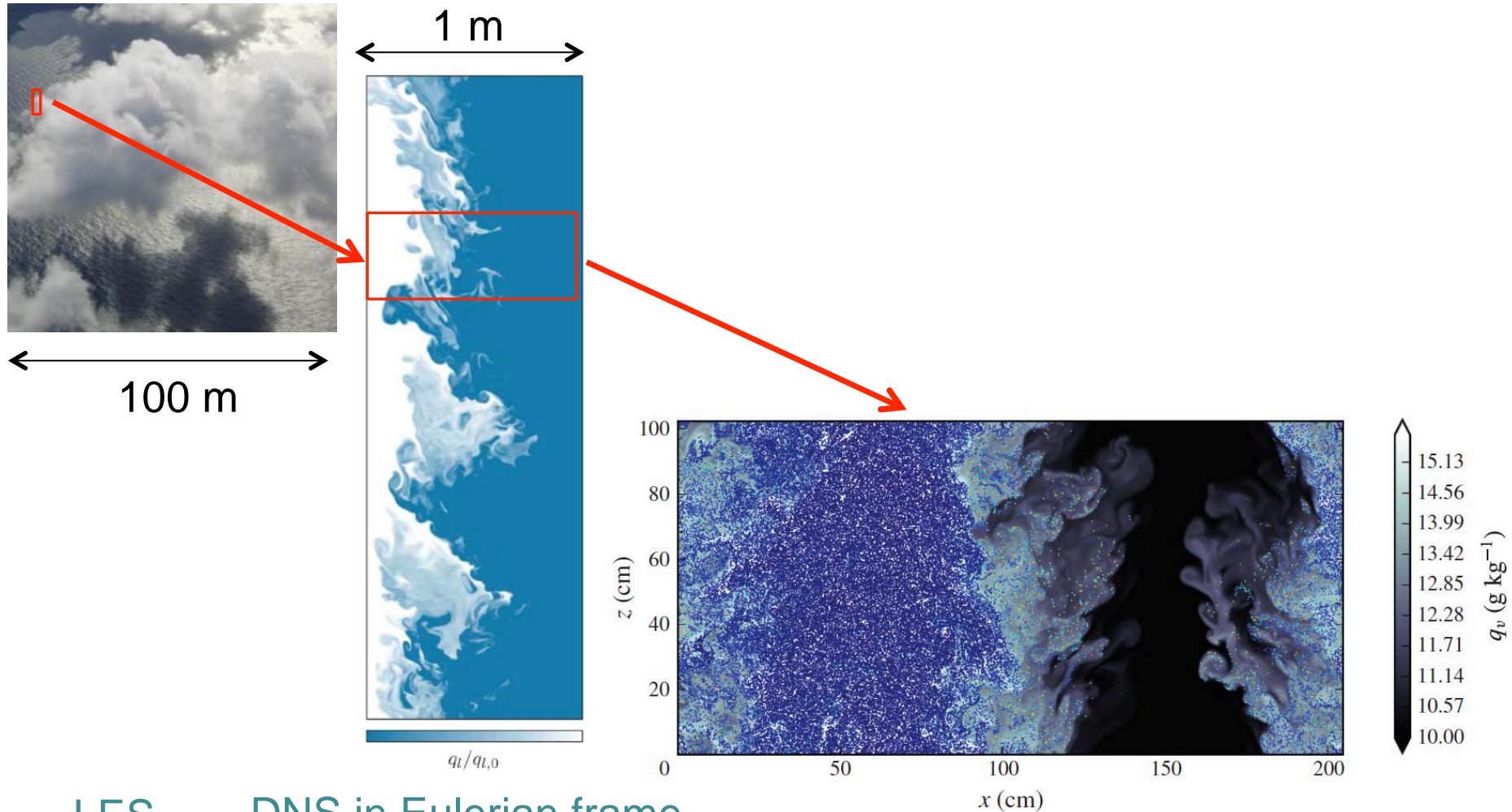


Trade wind cumuli over Barbados



How does the droplet size distribution at the edge of the cloud respond to the turbulent entrainment and subsequent mixing?

# DNS at the cloud interface



LES

DNS in Eulerian frame

Euler-Lagrangian DNS  
with phase changes

*Sardina et al.*  
*J. Atmos. Sci.*, 2018

*Abma et al.*  
*J. Atmos. Sci.*, 2013

# Coupled Euler-Lagrange model

$$\begin{aligned} \nabla \cdot \vec{u} &= 0 \\ \partial_t \vec{u} + (\vec{u} \cdot \nabla) \vec{u} &= -\frac{1}{\rho_0} \nabla p + \nu \nabla^2 \vec{u} + \vec{f} \\ \partial_t T + (\vec{u} \cdot \nabla) T &= \kappa \nabla^2 T + \frac{L}{c_p} C_d \\ \partial_t q_v + (\vec{u} \cdot \nabla) q_v &= \kappa_q \nabla^2 q_v - C_d \\ \vec{f} &= g \left[ \frac{T - T_0}{T_0} + \epsilon (q_v - q_{v0}) - q_l \right] \vec{e}_z \end{aligned}$$

Velocity

Temperature

Water Vapor  
Content

$$\begin{aligned} S(T) &= \frac{q_v}{q_{vs}(T)} - 1 \\ q_{vs}(T) &= A \exp(-B/T) \end{aligned}$$

$$C_d(\vec{x}, t) = \frac{1}{\rho_0 a^3} \sum_{\beta=1}^{\Delta} \frac{dm_l(\vec{X}_\beta, t)}{dt}$$

$$\begin{aligned} \frac{d\vec{X}}{dt} &= \vec{V}(\vec{X}, t) \\ \frac{d\vec{V}}{dt} &= \frac{1}{\tau_p} [\vec{u}(\vec{X}, t) - \vec{V}] + \vec{g} \\ r(\vec{X}, t) \frac{dr(\vec{X}, t)}{dt} &= KS(\vec{X}, t) \end{aligned}$$

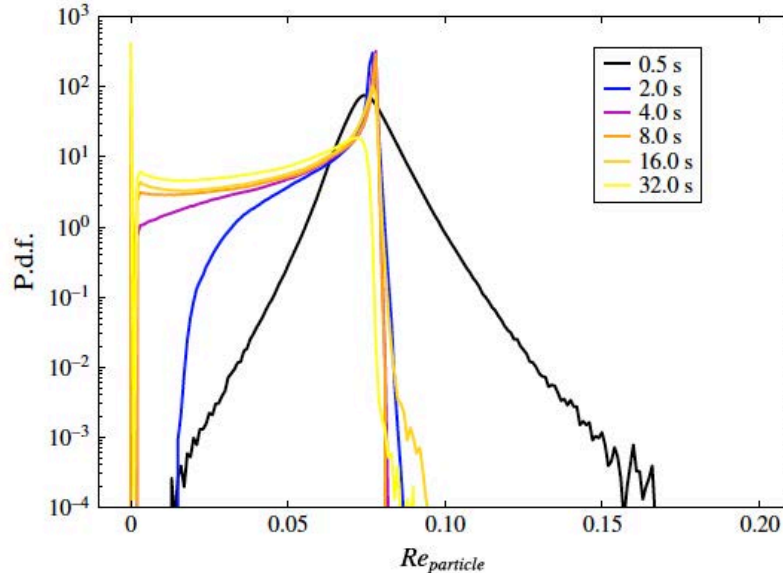
Droplet  
Dynamics

Diffusional  
Growth

Water vapor saturation mixing ratio  $q_{vs}$  via Clausius-Clapeyron equation is now a function of T

# Simplifications

- Stokes drag term only, no history effects (particle Reynolds number  $< 0.1$ )



$$Re_{particle} = \frac{|u_i(X_j, t) - V_i(X_j, t)|d}{\nu}$$

- Droplet collisions are neglected (collision time is for present conditions  $\sim 1$  h)

$$\tau_{1,2} \sim (n\pi(d_1 + d_2)^2 |v_{t,1} - v_{t,2}| \epsilon_{1,2})^{-1}$$

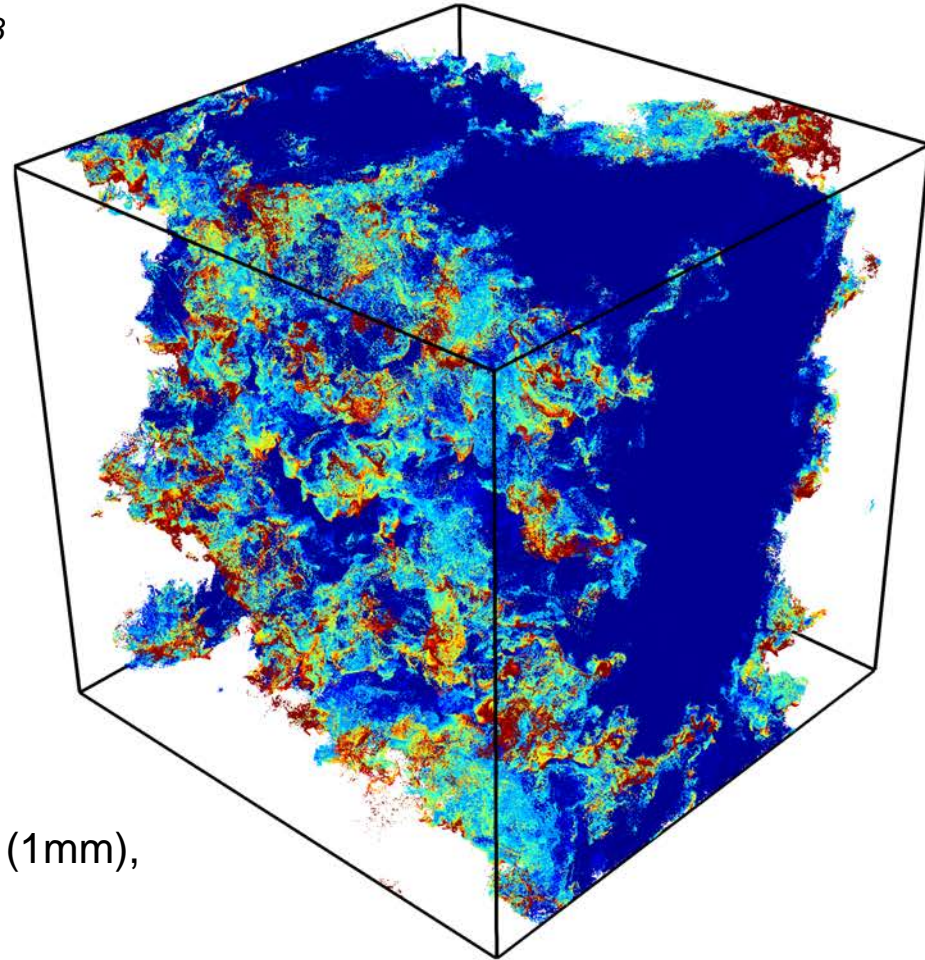
*Devenish et al. QJRMS 2012; Onishi et al., J. Atmos. Sci. 2015; Saito & Gotoh, New J. Phys. 2018*

- No two-way coupling (small droplet number density  $\sim 100 \text{ cm}^{-3}$ )
- Initially monodisperse droplet ensemble *Yang et al. ACP 2018*
- Constant material parameters (viscosity, conductivity,..) since T difference is a few degrees only



# Effect of domain size

*Kumar et al., submitted, 2018*



Cubic box with statistically stationary turbulence

Box size varies from 0.128 to 2.048 m

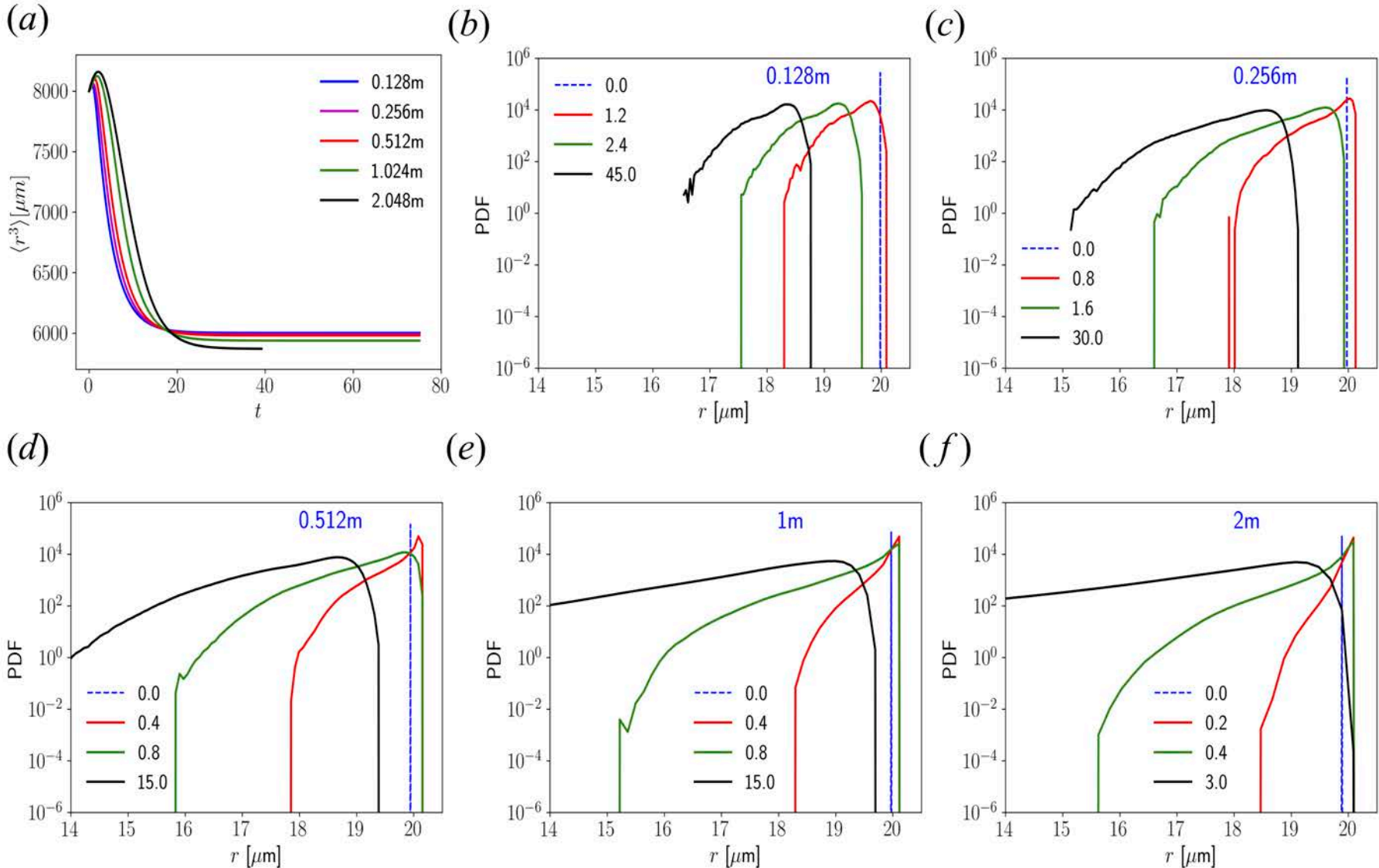
Droplet number varies  $1.05 \times 10^5$  to  $4.33 \times 10^8$

Same mean dissipation rate, Kolmogorov length (1mm),  
liquid water content & total water content

Same slab-like initial condition and grid resolution  
(periodic b.c.)

Entrainment and mixing evolution for a minute or more

# Liquid water content and size distributions



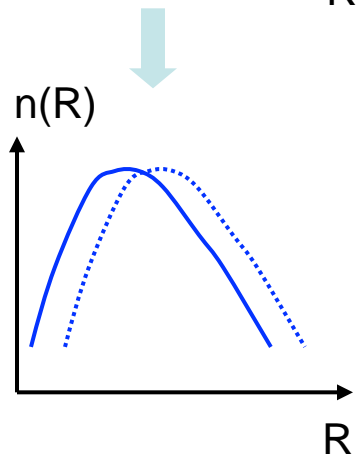
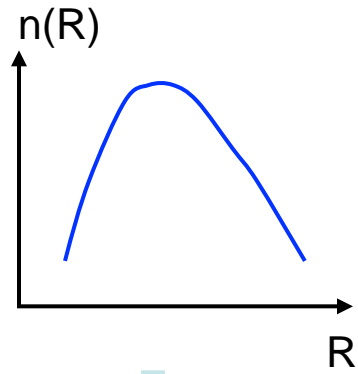
complete evaporation of  
some droplets

# Mixing diagrams

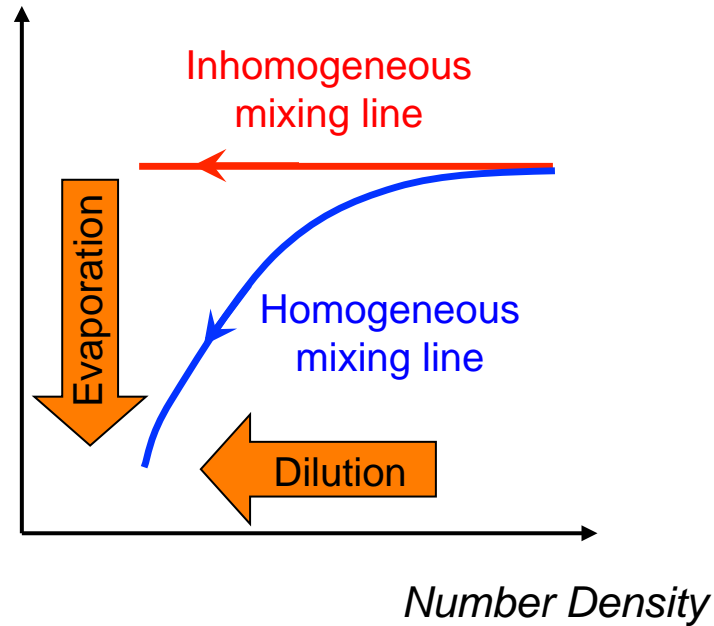
Burnet & Brenguier, *J. Atmos. Sci.* 2007; Lehmann, Siebert & Shaw, *J. Atmos. Sci.* 2009

Homogeneous mixing

$$Da \ll 1$$

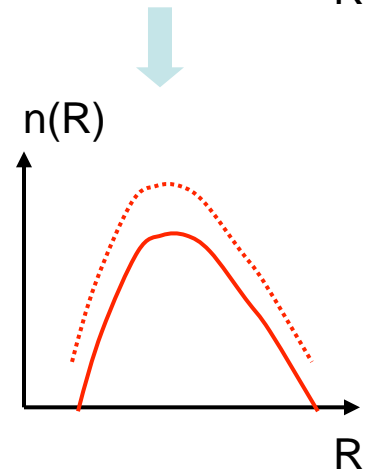
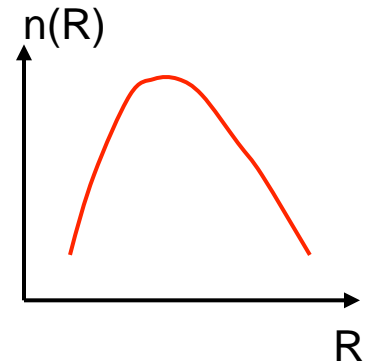


Mean Cubic Diameter



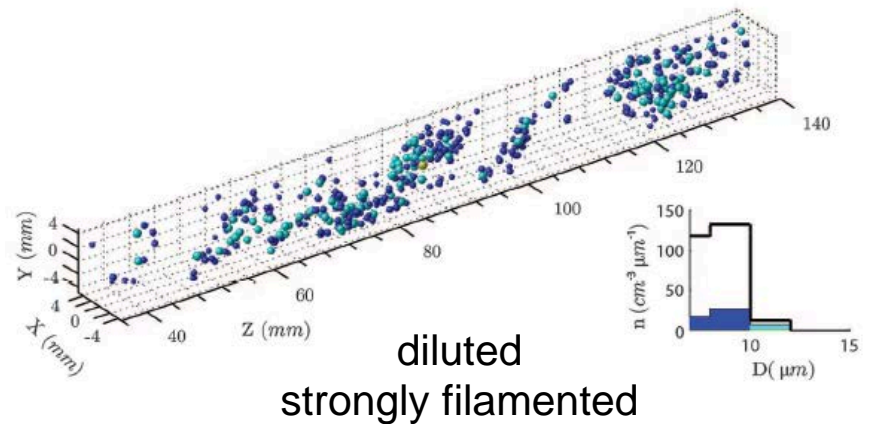
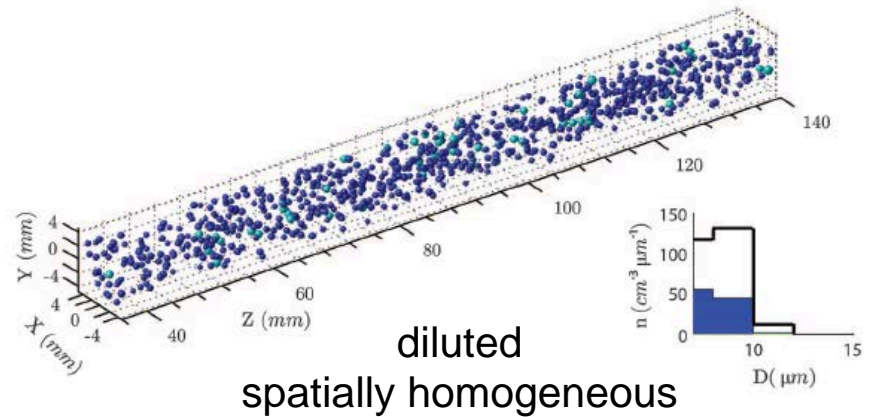
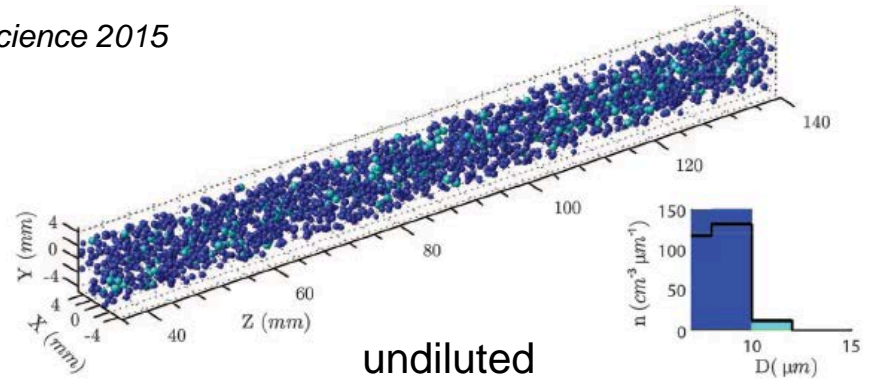
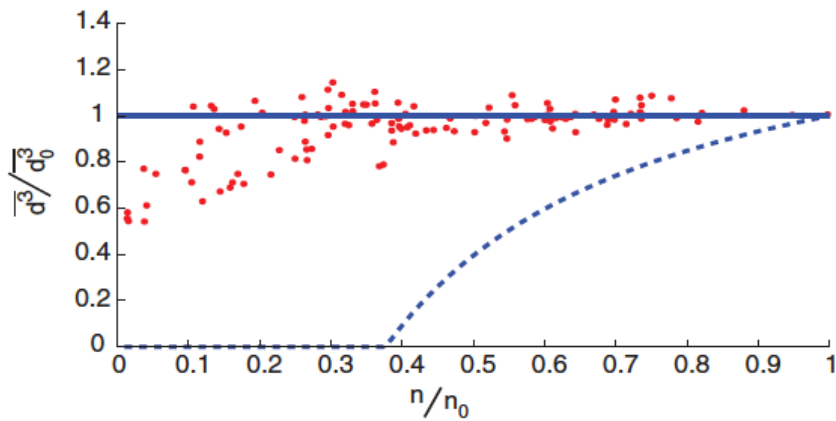
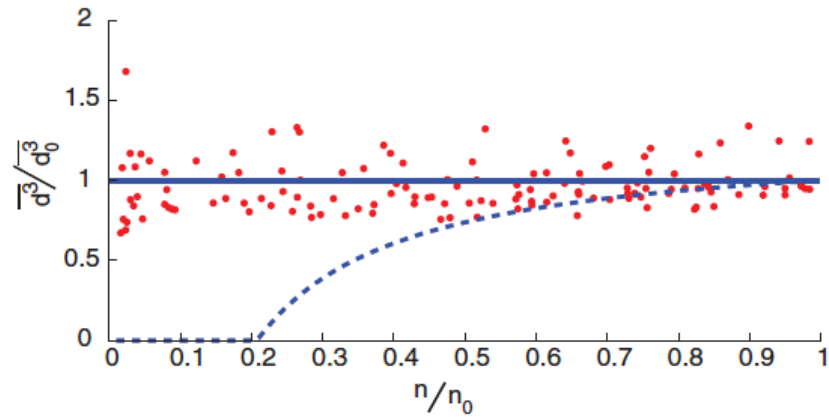
Inhomogeneous mixing

$$Da \gg 1$$



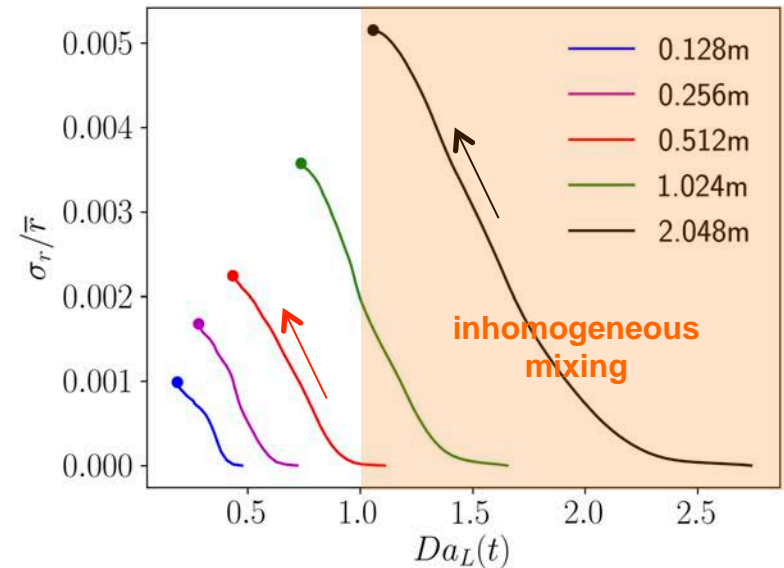
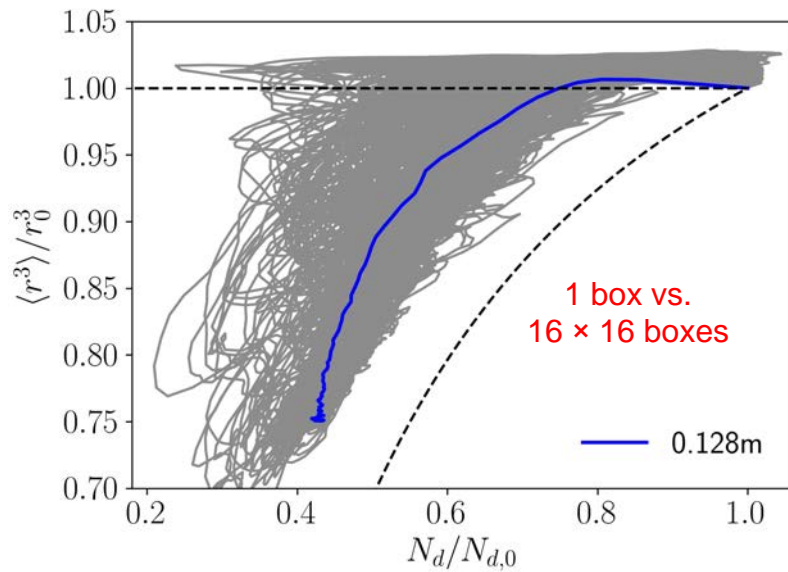
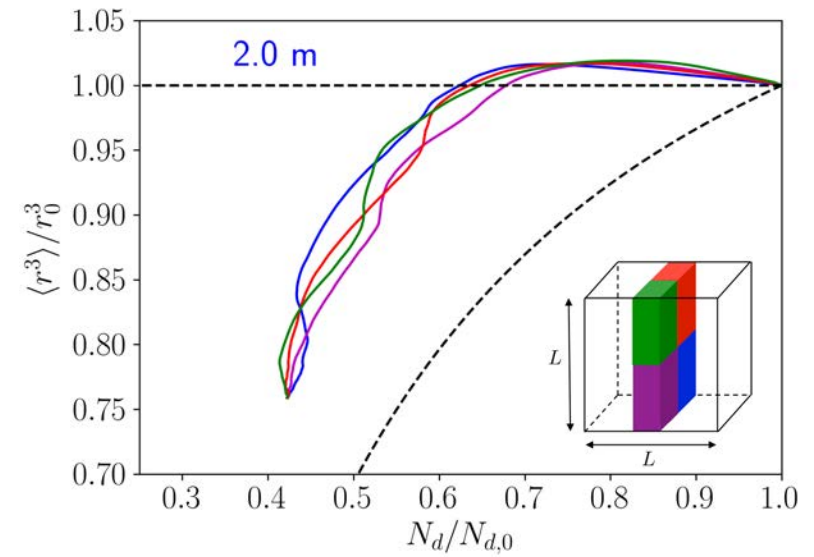
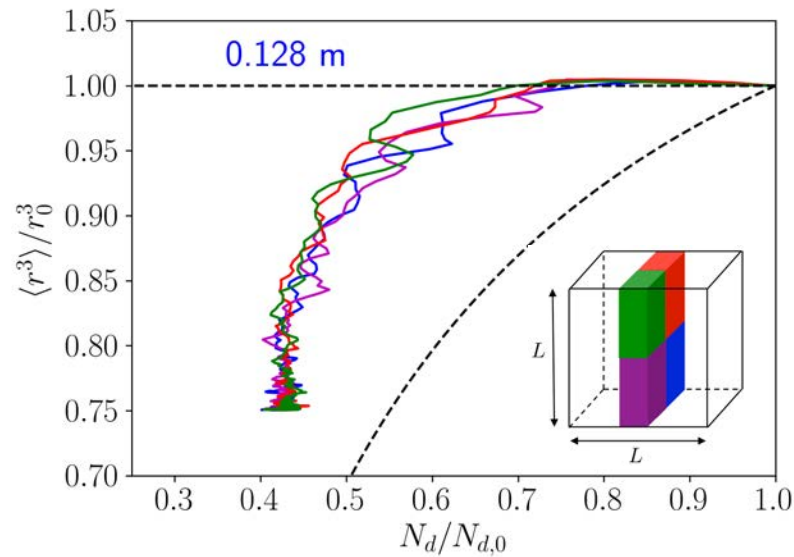
# Holographic airborne measurements

Beals et al., Science 2015



Confirmation of strong inhomogeneous mixing at cloud edge

# Mixing diagrams

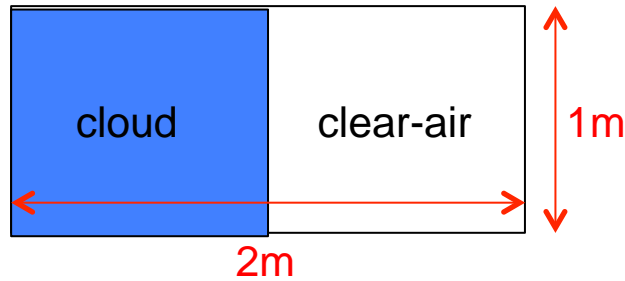


Inhomogeneous mixing effects increase with domain size

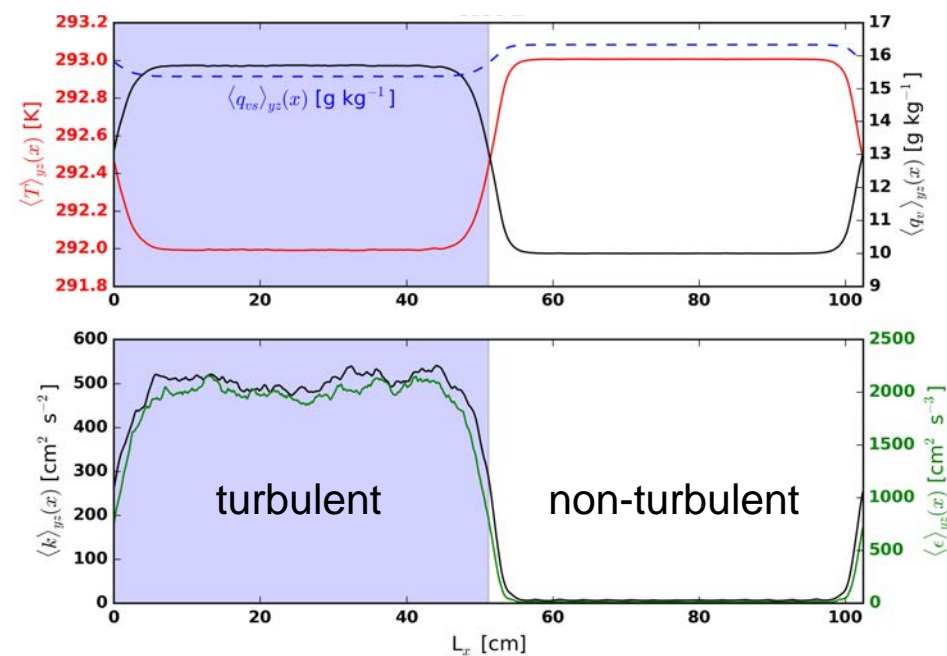
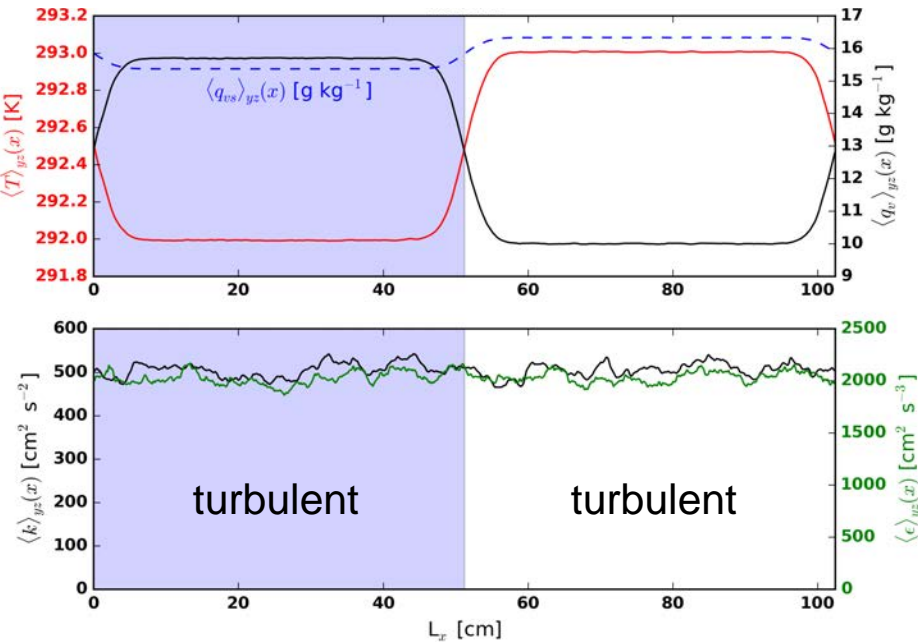
# Shear-free mixing layer with phase changes

Tordella & Iovieno, *J. Fluid Mech.* 2006

TTI



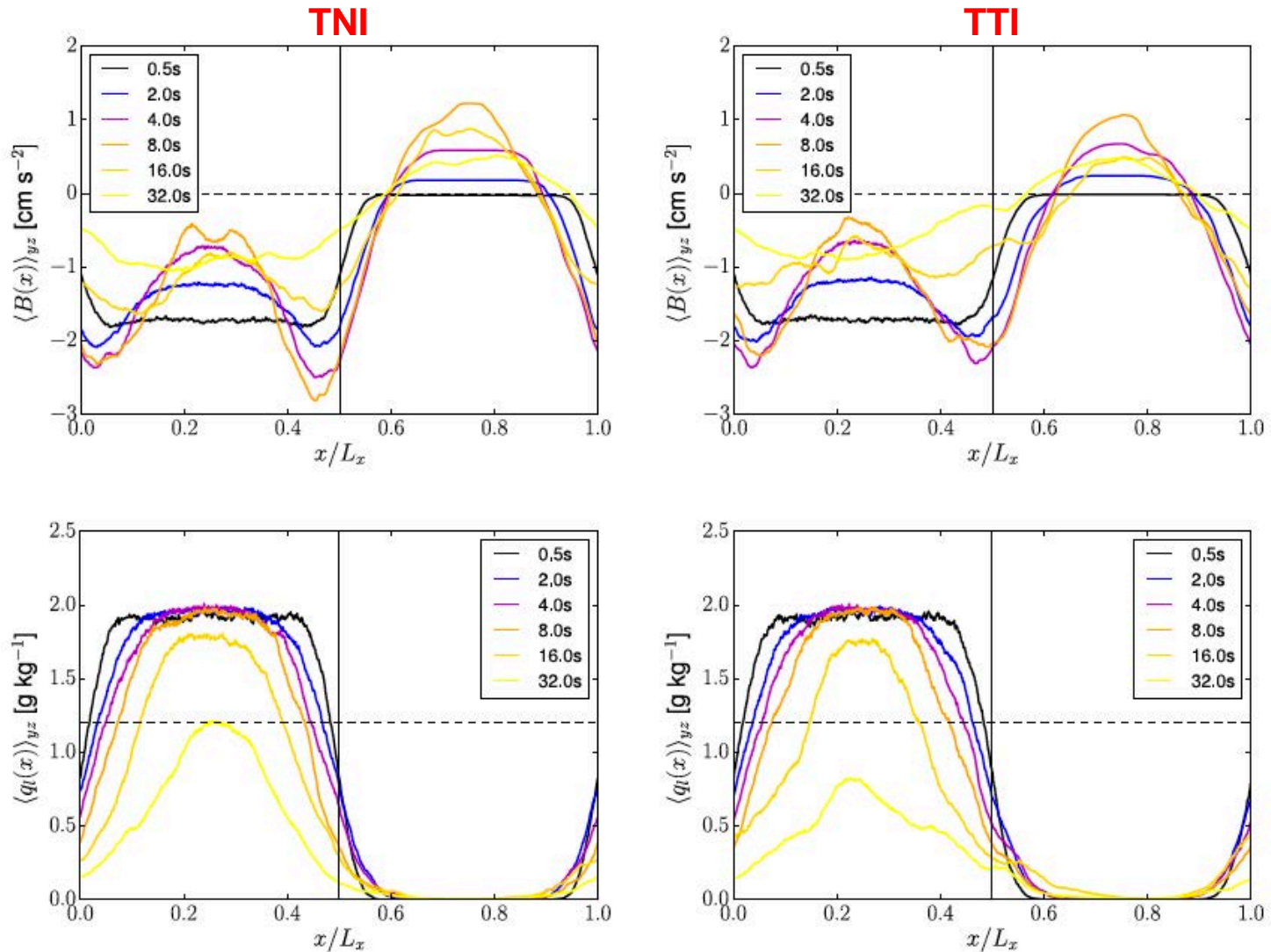
TNI



Freely decaying turbulence = dissolving cloud

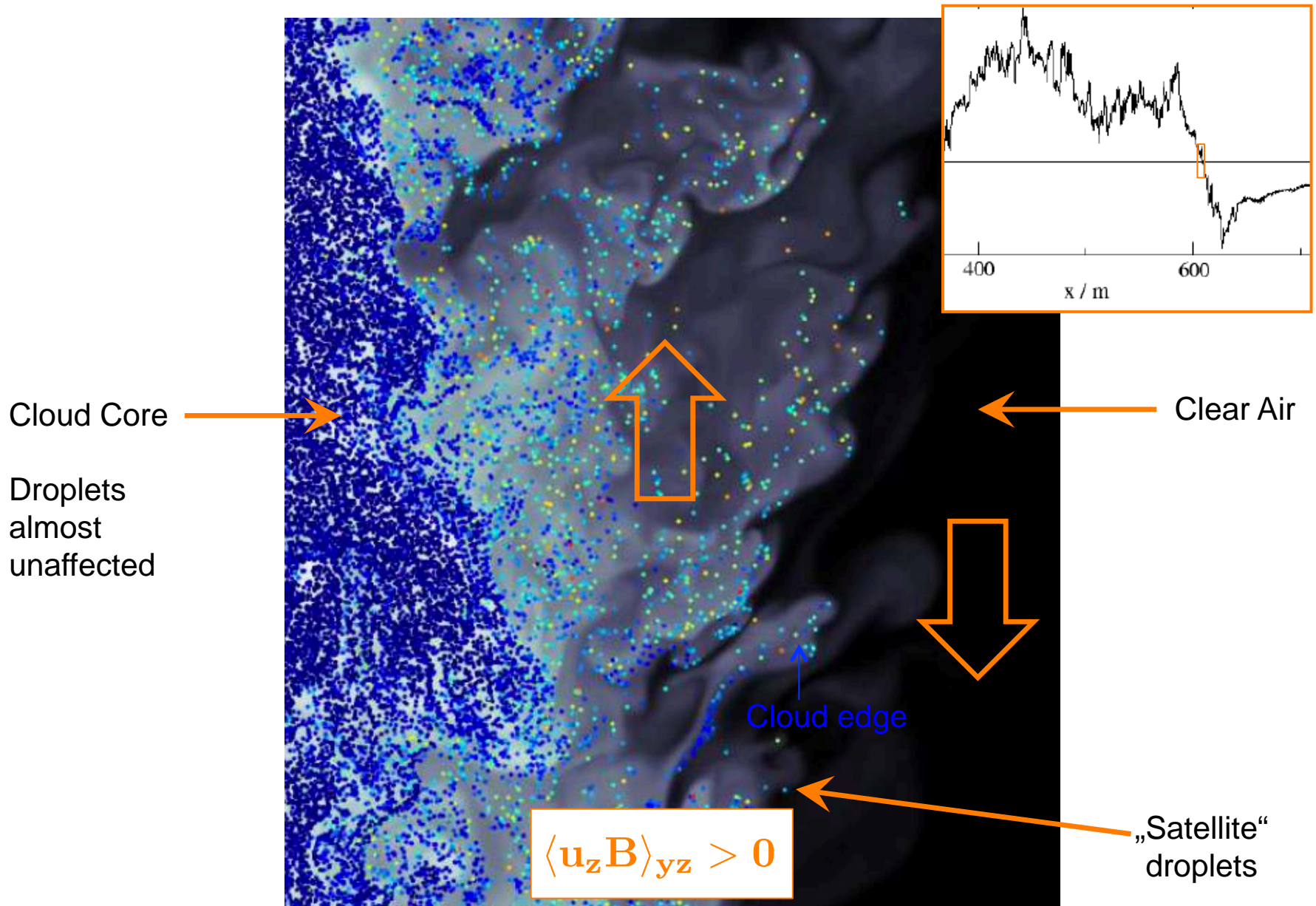
# Entrainment process

Götzfried et al., J. Fluid Mech. 2017



Different initial flow conditions affect large scale turbulence only slightly

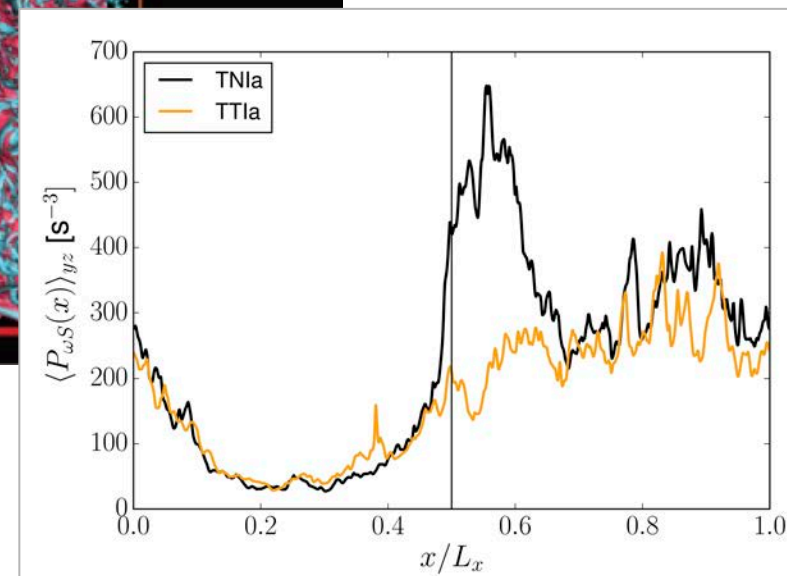
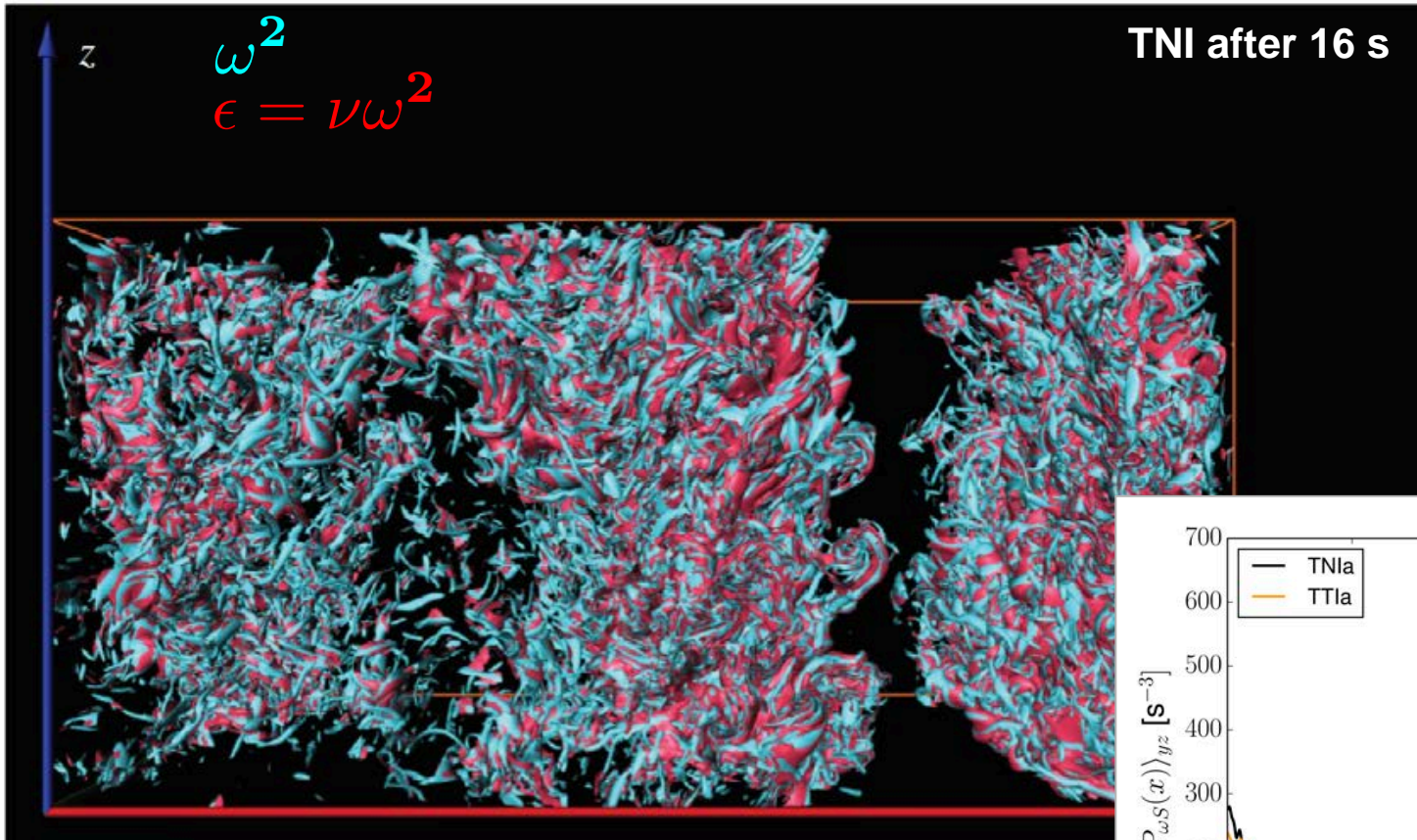
# Evaporative cooling induces shear layer





# Enstrophy production

Götzfried et al., J. Fluid Mech. 2017



Different initial turbulent flow fields affect small-scale mixing significantly



- Coupled Euler-Lagrangian model to study interplay between turbulence and droplet dynamics at cloud interface
- Effect of different turbulence levels on mixing process remains small
- Increasing box size leads to increase of inhomogeneous mixing and droplet size dispersion
- Evaporative cooling causes downdraught at interface

B. Kumar, F. Janetzko, JS, and R. A. Shaw, *New J. Phys.* 14, 115020 (2012)

B. Kumar, JS, and R. A. Shaw, *Theor. Comput. Fluid Dyn.* 27, 361 (2013).

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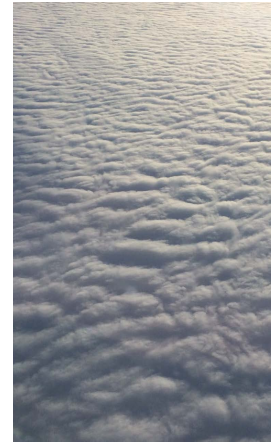
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# Outlook

## Mesoscale

- Extensions of moist Boussinesq models
  - large-scale flow forcing
  - rotation
  - radiative forcing
- Effective parametrization in larger-scale models



## Microscale

- Activation of cloud condensation nuclei in an environment with highly fluctuating supersaturation
- Radiative cooling and collision impact on droplet growth

